

7 Continuous charge distributions

$$d\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_0 dQ}{r^2} \hat{r} = q_0 d\vec{E} \qquad d\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{dQ}{r^2} \hat{r}$$

$$\vec{E} = \int d\vec{E} \qquad E_x^{line} = \frac{1}{4\pi\epsilon_0} \frac{\lambda L}{x\sqrt{x^2 + L^2/4}} \qquad dQ = \lambda dl = \sigma dA = \rho dV$$

$$E_z^{ring} = \frac{\lambda}{2\epsilon_0} \frac{Rz}{(z^2 + R^2)^{3/2}}$$

7.a RHK Exercises

25-17 Consider the rod with total charge Q , and the point charge q_0 in Fig. 25-11. Where can you place a second point charge Q (same charge as the rod), so that q_0 is in equilibrium? Solve this problem assuming that (a) q is positive and (b) q is negative

25-19 Assume the rod in Fig. 25-11 instead has a charge density λ on the top half of the rod and a uniform charge density $-\lambda$ on the bottom half of the rod. Find the force on q_0 .

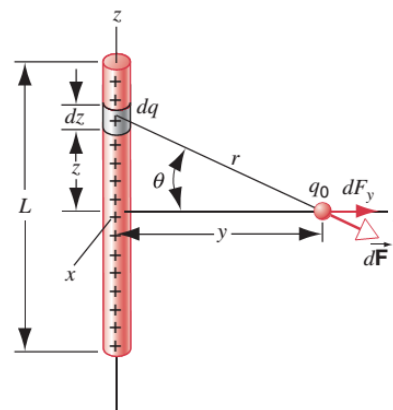


FIGURE 25-11. A uniformly charged rod.

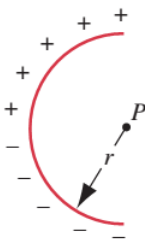


FIGURE 26-28. Exercise 16.

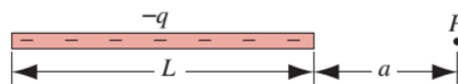


FIGURE 26-29. Exercise 18.

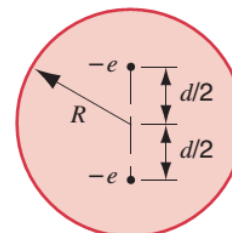


FIGURE 26-36. Exercise 40.

26-XX A circular disk of radius R has a uniform area charge density σ . Determine the electric field along the axis of the disk as a function of the distance z from the disk.

26-28 A thin glass rod is bent into a semicircle of radius r . A charge $+q$ is uniformly distributed along the upper half and a charge $-q$ is uniformly distributed along the lower half, as shown in Fig. 26-28. Find the electric field $2\vec{E}$ at P , the center of the semicircle.

26-29 An insulating rod of length L has charge q uniformly distributed along its length, as shown in Fig. 26-29. (a) What is the linear charge density of the rod? (b) Find the electric field at point P a distance a from the end of the rod. (c) If P were very far from the rod compared to L , the rod would look like a point charge. Show that your answer to (b) reduces to the electric field of a point charge for $a \gg L$.

26-40 Figure 26-36 shows a Thomson atom model of helium ($Z = 2$). Two electrons, at rest, are embedded inside a uniform sphere of positive charge $2e$ with a fixed radius R . Find the distance d between the electrons so that the configuration of the electrons is in static equilibrium.

7.b RHK Problems

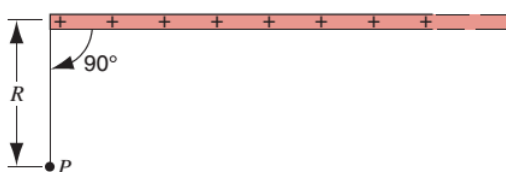


FIGURE 26-39. Problem 6.

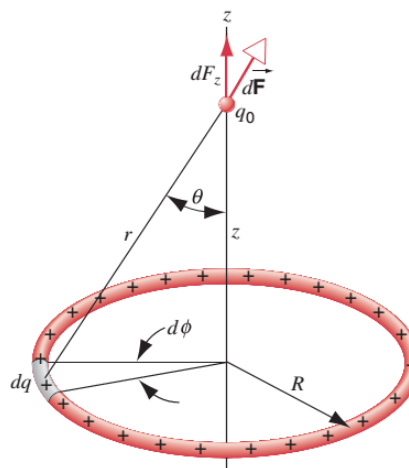


FIGURE 25-12. A uniformly charged ring. To find the force on a point charge q_0 , we consider the ring to consist of many individual charge elements such as dq .

25-3 Consider the ring of charge in Fig. 25-12. Suppose that the charge q is not distributed uniformly over the ring but that charge q_1 is distributed uniformly over half the circumference and charge q_2 is distributed uniformly over the other half. Let $q_1 + q_2 = q$. (a) Find the component of the electric field at any point on the axis directed along the axis and compare with the uniform case. (b) Find the component of the electric field at any point on the axis perpendicular to the axis and compare with the uniform case.

25-6 A “semi-infinite” insulating rod (Fig. 26-39) carries a constant charge per unit length of λ . Show that the electric field at the point P makes an angle of 45° with the rod and that this result is independent of the distance R .

25-7 A thin nonconducting rod of finite length L carries a uniform linear charge density $+\lambda$ on the top half and a uniform charge density $-\lambda$ on the bottom half; compare to Fig. 25-11. (a) Use a symmetry argument to determine the direction of the electric field at P (the location of q_0 in Fig. 25-11) due to the rod. (b) Find \vec{E} at P . (c) Take the limit of this expression for large y . How does it depend on y ? What does it remind you of?

25-8 A nonconducting hemispherical cup of inner radius R has a total charge q spread uniformly over its inner surface. Find the electric field at the center of curvature. (Hint: Consider the cup as a stack of rings.)

25-12 An electron is constrained to move along the axis of the ring of charge discussed in Fig. 25-12. Show that the electron can perform small oscillations, through the center of the ring, with a frequency given by

$$\omega = \sqrt{\frac{eq}{4\pi\epsilon_0 m R^3}} \tag{7.1}$$