## 4 Heat and the First Law of Thermodynamics

$$\begin{split} Q &= C\Delta T = mc\Delta T & Q = mL & \Delta E_{int} = Q - W \\ C_V &= \frac{d}{2}R & C_p = \left(1 + \frac{d}{2}\right)R & \gamma = \frac{C_p}{C_V} = 1 + \frac{2}{d} \\ c_{H20} &= 4190 \sim 4000 \text{ J/(kg K)} & L_f^{H2O} = 333 \text{ kJ/ kg} & L_v^{H2O} = 2256 \text{ kJ / kg} \end{split}$$

## 4.a RHK Exercises

**23-17** A 100 g copper bowl contains 200 g of water, with both at 27 °C. A very hot 300 g copper cylinder is dropped into the water. This causes the water to boil, with 5 g being converted to steam, and the final temperature of the entire system is 100 °C. (*a*) How much heat was transferred to the water? (*b*) How much to the bowl? (*c*) What was the original temperature of the cylinder? (First use  $c_{Cu}$ ,  $c_{H2O}$  and  $L_v$  algebraically. Then take the values  $c_{Cu} \sim 500$ ,  $c_{H2O} \sim 4000$  J/(kg K), and  $L_v \sim 2000$  kJ/kg.)

**23-20** What mass of steam at 100 °C must be mixed with 150 g of ice at 0 °C, in a thermally insulated container, to produce liquid water at 50 °C? (Round  $L_f \sim 300 \text{ J/g}$ )

**23-35** In an experiment, 2 mol of oxygen ( $O_2$ ) are heated at constant pressure starting at 300 K. How much heat must be added to the gas to double its volume?



**23-40** Gas within a chamber passes through the cycle shown in Fig. 23-34. Determine the net heat added to the gas during process CA if  $Q_{AB} = 20$  J,  $Q_{BC} = 0$ , and  $W_{BCA} = 15$  J.

**23-42** A sample of *n* moles of an ideal gas undergoes an isothermal expansion. Find the heat flow into the gas in terms of the initial and final volumes and the temperature.

**23-43** A quantity of ideal gas occupies an initial volume  $V_0$  at a pressure  $p_0$  and a temperature  $T_0$ . It expands to volume  $V_1$  (a) at constant pressure, (b) at constant temperature, and (c) adiabatically. Graph each case on a pV diagram. In which case is Q greatest? Least? In which case is W greatest? Least? In which case is  $\Delta E_{int}$  greatest? Least?

**23-46** Gas within a chamber undergoes the processes shown in the PV diagram of Fig. 23-36. Calculate the net heat added to the system during one complete cycle.

## 4.b RHK Problems



**23-8** A flow calorimeter is used to measure the specific heat of a liquid. Heat is added at a known rate to a stream of the liquid as it passes through the calorimeter at a known rate. Then a measurement of the resulting temperature difference between the inflow and the outflow points of the liquid stream enables us to compute the specific heat of the liquid. A liquid of density  $\rho$  flows through a calorimeter with speed v and a cross-section area A. Heat is added by means of a X Watt electric heating coil, and a temperature difference of  $\Delta T$  is established in steady-state conditions between the inflow and the outflow points.

(a) Draw a diagram of this device.

(b) Find the specific heat of the liquid.

**23-9** Water standing in the open at 27 °C evaporates because of the escape of some of the surface molecules. The heat of vaporization is approximately equal to  $\epsilon n$ , where  $\epsilon$  is the average energy of the escaping molecules and n is the number of molecules per kilogram.

(a) Explain why this is true.

(b) Determine the value of  $\epsilon$ .

(c) What is the ratio of  $\epsilon$  to the average kinetic energy of H<sub>2</sub>O molecules, assuming that the kinetic energy is related to temperature in the same way as it is for gases?

**23-18** Figure 23-38a shows a cylinder containing gas and closed by a movable piston. The cylinder is submerged in an ice–water mixture. The piston is quickly pushed down from position 1 to position 2. The piston is held at position 2 until the gas is again at 0  $^{\circ}$  C and then is slowly raised back to position 1. Figure 23-38b is a PV diagram for the process.

(a) If 100 g of ice are melted during the cycle, how much work has been done by the gas?

(b) Identify which of the processes is *isochoric*, which is *isothermal* and which is *adiabatic*.

(c) Find an expression for W as a function of the number of moles n of gas, the ice water temperature T, the volume ratio  $r = V_2/V_1$ , and the adiabatic constant  $\gamma$ .

**23-40** A cylinder has a well-fitted, 2 kg metal piston whose cross-sectional area is 2 cm<sup>2</sup> (Fig. 23-40). The cylinder contains water and steam at constant temperature. The piston is observed to fall slowly at a rate of 0.30 cm/s because heat flows out of the cylinder through the cylinder walls. As this happens, some steam condenses in the chamber. The density of the steam inside the chamber is  $6 \times 10^4$  g/cm<sup>3</sup> and the atmospheric pressure is 1.0 atm.

(a) Calculate the rate of condensation of steam.

- (b) At what rate is heat leaving the chamber?
- (c) What is the rate of change of internal energy of the steam and water inside the chamber?