

3 Work and Internal Energy

$$\begin{array}{lll}
 Nk = nR & E_{int} = \frac{d}{2}nRT & W = \int p dV = \text{(work done by the gas)} \\
 \text{Isothermal:} & pV = \text{const.} & W = nRT \ln \frac{V_f}{V_i} \\
 \text{Adiabatic:} & pV^\gamma = \text{const.} & W = -\frac{p_i V_i}{\gamma - 1} \left[\left(\frac{V_i}{V_f} \right)^\gamma - 1 \right] = -\frac{1}{\gamma - 1} (p_f V_f - p_i V_i)
 \end{array}$$

3.a RHK Exercises

23.25 . Suppose that a sample of gas expands from 2.0 to 8.0 m³ along the diagonal path in the PV diagram shown in Fig. 23-33. It is then compressed back to 2.0 m³ along either path 1 or path 2. Compute the net work done by the gas for the complete cycle in each case.

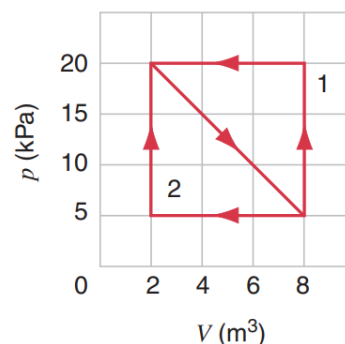


FIGURE 23-33. Exercise 25.

23.26 (Modified) An ideal gas that occupies volume V_1 at pressure p_1 is expanded isothermally until $V_2 = 3V_1$ and then cooled at constant pressure until it returns to its initial volume. (a) Compute the work done on the gas. (b) Calculate the change in internal energy of the gas.

23.30 An air compressor takes air at T_1 and pressure p_1 and delivers compressed air at pressure $p_2 = 2p_1$. The compressor operates at 200 W of useful power. Assume that the compressor operates adiabatically. (a) Find the temperature of the compressed air. (b) How much compressed air, in liters, is delivered each second?

3.b RHK Problems

23.14 The van der Waals equation of state

$$\left(p + \frac{an^2}{V^2} \right) (V - nb) = nRT \tag{3.1}$$

is a modification of the ideal gas law that incorporates the finite size b of molecules, and the weak attraction a between them. (The constants a and b are usually determined experimentally.) Calculate the work done by n moles of a van der Waals gas in an isothermal expansion from volume V_i to V_f .

23.16 A room of volume V is filled with diatomic ideal gas (air) at temperature T_1 and pressure p_0 . The air is heated to a higher temperature T_2 , the pressure remaining constant at p_0 because the walls of the room are not airtight. Show that the internal energy content of the air remaining in the room is the same at T_1 and T_2 . If we add no energy to the air inside, why bother to light the furnace?

23.XX An ideal gas with N particles undergoes a thermodynamic process from (T_0, V_0) to (T_f, V_f) . Along the process, the quantity T/V^2 is held constant. (a) What does the process look like on a PV diagram? (b) Calculate the work done by the gas, and the change in internal energy.